

SELF AND PEER ASSESSMENT

How can I use assessment to improve learning?

Introduction

“... self-assessment by students, far from being a luxury, is in fact an essential component of formative assessment. Where anyone is trying to learn, feedback about their efforts has three elements—the desired goal, the evidence about their present position, and some understanding of a way to close the gap between the two. All three must to a degree be understood by anyone before they can take action to improve their learning.” (Black & Wiliam, 1998)

This is particularly true when the focus of the assessment is on the processes involved in IBL. Many students do not understand their nature and importance in mathematics. If a student’s goal is only to get ‘the right answer’, then she will not attend to the deeper purposes of the lesson.

This module encourages discussion of the following issues:

- How can we help students to become more aware of IBL processes, and their importance in problem solving?
- How we can encourage students to take more responsibility for their own learning of IBL processes?
- How can students be encouraged to assess and improve each other’s work?

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Acknowledgement:

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Swan, M; Pead, D (2008). *Professional development resources*. Bowland Maths Key Stage 3, Bowland Trust/ Department for Children, Schools and Families. Obtainable in the UK from: <http://www.bowlandmaths.org.uk>.

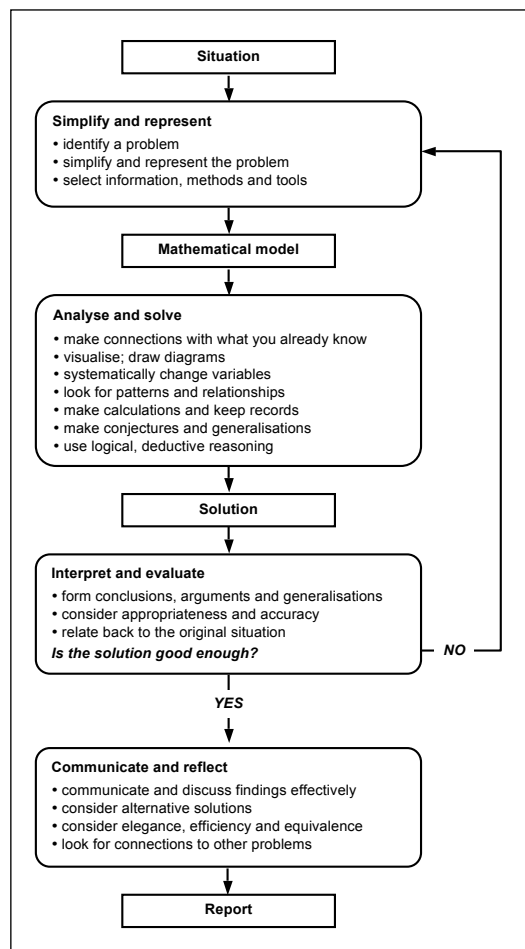
Swan, M; (2005). *Improving Learning in Mathematics*, challenges and strategies, Department for Education and Skills Standards Unit. Obtainable in the UK from http://tlp.excellencegateway.org.uk/pdf/Improving_learning_in_maths.pdf

ACTIVITY A: EXPLORE HOW STUDENTS MAY BE MADE AWARE OF IBL PROCESSES

Time needed: 20 minutes.

Inquiry-based learning (IBL), as has been said in earlier modules, is about engaging students' curiosity in the world and the ideas that surround them. During Mathematics and Science lessons, we want students to move from being passive receivers of factual knowledge to active engagement in using inquiry-based learning processes. This means using their conceptual knowledge to tackle new, unfamiliar problems, in similar ways to those used by scientists and mathematicians. Students will begin to observe and pose questions about the world around them. When these questions are too complex, they will engage in a modeling process: simplify and represent the situation; analyze data; interpret and evaluate findings, communicate findings with others (See figure) and reflect on the outcomes. For many students, these are new and unfamiliar learning goals and will require a shift in the way students approach their learning.

This activity begins to consider some ways in which students may be helped to appreciate these new learning goals and thus begin to consider their value and importance.



Handout 1 presents a number of suggestions made by teachers that could help students become more aware of IBL processes.

- Discuss the advantages and disadvantages of each suggestion.
- Can you think of any other ways of making students more aware of these processes?

This module considers some of these suggestions in more depth.

Handout 1: Helping students to become aware of IBL learning goals

1. Using a poster or handout

Make a poster showing the generic list of processes and display this on the classroom wall. Refer to this habitually, while students work on unstructured problems, so that they become more aware that your goals for the lesson are for them to become more able to simplify and represent, analyse and solve, interpret and evaluate, communicate and reflect.

2. Creating task-specific hints

Before the lesson, prepare some task-specific hints that apply IBL processes to the particular problem in hand. When students are stuck, give them the appropriate hint either on paper or orally. For example, you could ask: "Can you use a table or graph to organise this data?"; "What is fixed and what can you change in this problem?"; "What patterns can you see in this data?".

3. Asking students to assess provided samples of work

After students have worked on a task, present them with some prepared, sample responses from other students. These solutions provide alternative strategies students may not have considered and may also contain errors. Ask students to pretend they are examiners. The students rank order these solutions, along with their own response, giving explanations as to why they think one response is better than another.

4. Using prepared 'progression steps'

Students evaluate sample responses as in (3) above, but this time you also provide them with prepared progression steps that highlight the IBL processes. Students use these to evaluate the work. End the lesson by sharing what has been learned from this process.

5. Asking students to assess each other's work.

After tackling a task in pairs, students exchange their work. Each pair of students is given the work of another pair. Students make suggestions for ways of improving each solution and stick these on the work using "sticky" notes. These comments are passed back to the originators, who must then produce a final, improved version based on the comments received. This is a more challenging strategy for the teacher than (3), as the issues that arise will be less predictable.

6. Students interview each other about the processes they have used.

When students have finished working on a task, ask them to get into pairs. Each member of a pair interviews his or her partner about their approach and the processes they have used while working on the task. The teacher may provide some pre-prepared questions to assist in this. After noting down the replies, students change roles. Suitable questions might be:

- What approach did you take?
- Which processes did you use (from a provided list)?
- How could this work be improved?
- What could you have done differently?
- Is there still something you are confused by?

ACTIVITY B: CONSIDER HOW STUDENTS CAN LEARN FROM SAMPLE WORK

Time needed: 30 minutes

One powerful strategy for enabling students to appreciate different learning goals is to ask them to assess the work of others. This role shift has several learning advantages:

- **It encourages students to consider alternative methods.** In many Mathematics and Science lessons, students are only presented with one method for doing each task. They do not therefore come to appreciate the strengths and weaknesses of alternative approaches.
- **It encourages students to consider methods that they would have not have normally chosen.** When solving mathematical problems, for example, research shows us that many students do not choose to use algebra or graphical methods.
- **It enables students to see the purpose of IBL tasks more clearly.** Many students just consider the purpose of the lesson as to 'get the right answer'. In assessing work, particularly against provided criteria, students are encouraged to appreciate the *relative qualities* of different methods.

This activity involves watching a video clip of a lesson in which secondary students assess student work that has been provided by the teacher. This work was chosen to represent five different approaches to the problem *Text Messaging*, on Handout 2. Before the lesson, the students had been asked to attempt the problem individually, without help. In this follow-up lesson, students first try to comprehend the sample work then they evaluate it.

Before watching the video clip, do the task *Text Messaging* yourself, and consider the sample work with a group of colleagues, if possible.

- What IBL processes are evident in the sample work?
- Anticipate the issues that will arise when this sample work is assessed by students.

Now watch students as they assess the sample work, and then go on to improve their own work.

- What do aspects of the provided work do students attend to?
- What criteria do students use as they assess the sample work?
- What are students learning from the sample work?

Teachers sometimes comment that some students attend more to the neatness of the sample work than to the quality and communication of the reasoning employed. Other teachers are concerned that students will uncritically 'copy' sample work.

- How do you respond to these concerns?
- What criteria would you use for choosing sample work to use with students?

Handout 2: An assessment task and student responses

Text Messaging

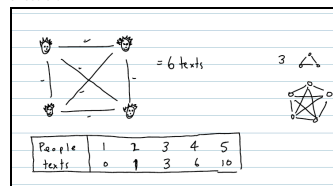


1. How many text messages are sent if four people all send messages to each other?
2. How many text messages are sent with different numbers of people?
3. Approximately how many text messages would travel in cyberspace if everyone in your school took part?
4. Can you think of other situations that would give rise to the same mathematical relationship?

Tom's answer

Celia sends one to Tracey = 1
 Tracey sends one to Celia = 1
 Tracey sends one to Maria = 1
 Maria sends one to Anne-Maria = 1
 Anne-Maria sends one to Celia = 1
 Celia sends one to Anne-Maria = 1
 Maria sends one to Tracey = 1
 Tracey sends one to Anne-Maria = 1
 Maria sends one to Celia = 1

Chris's answer



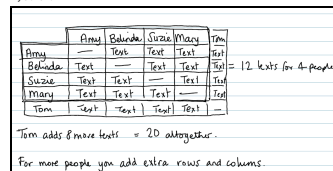
Marvin's answer

$4 \times 3 = 12$ So there are 12 messages with 4 people.
 With eight people there will be $8 \times 7 = 56$ messages
 With a thousand people there will be $1000 \times 999 = 999000$ messages
 The formula is number of people \times one less than this because you don't send a text to yourself.

Sam's answer

① For 4 people $\frac{4 \times 3}{2} = 6$
 ② $\frac{2 \times 1}{2} = 1$
 ③ $\frac{3 \times 2}{2} = 3$
 ④ $\frac{4 \times 3}{2} = 6$
 ⑤ $\frac{5 \times 4}{2} = 10$
 ⑥ $\frac{6 \times 5}{2} = 15$
 ⑦ $\frac{7 \times 6}{2} = 21$
 ⑧ $\frac{8 \times 7}{2} = 28$
 ⑨ $\frac{9 \times 8}{2} = 36$
 ⑩ Don't know.

Lily's answer



ACTIVITY C: DISCUSS HOW STUDENTS CAN LEARN FROM ASSESSING THEIR OWN WORK.

Time needed: 30 minutes

Often when students have finished a piece of work, they want to move on. They don't want to re-examine it, polish it, or present it so that other people can understand and follow their reasoning.

On the video, two teachers, Emma and Shane, ask their students to assess and improve each other's work. To help them do this, they provide some structured frameworks.

Emma uses the *Golden Rectangles* task and has collated a selection of her own students' work on this task into a poster. She has also simplified the assessment framework on **Handout 3** for use with her students. In the lesson, she asks groups of students to assess the work on the poster using the simplified framework. The headings on her framework are: "Represent", "Analyze", "Interpret", "Communicate". These correspond to the phases in the modeling diagram (shown in Activity A). On the video, students may be heard referring to a "traffic lights" scheme that Emma uses in her Mathematics lessons. Here, 'Green' means that students understand, while 'Red' means that they do not. 'Amber' lies in between.

Shane used the *Counting Trees* task and has prepared a less structured sheet to help his students assess each other's work. This sheet contains the questions: Did they choose a good method?; Was their reasoning correct?; Are their workings accurate?; Are their conclusions sensible?; Was their reasoning easy to follow?; What did you like about their work?; What would you like to see next time?

Familiarize yourself with the tasks.

Watch the video extracts of Shane's and Emma's lessons.

- What observations do students make about each other's work?
- How might this help them to improve their own work?

Compare Emma's simplified progression steps with Shane's less structured sheet.

- What are the advantages and disadvantages of each method for helping students to reflect on and improve their work?

Compare the use of work from within the students' own class to the use of the sample responses used in Activity B.

- What are the advantages and disadvantages of each method?

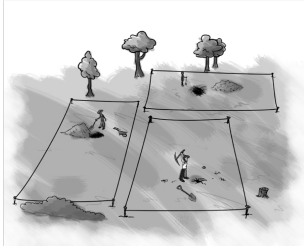
The assessment frameworks may help students to develop an awareness of how IBL processes relate to particular tasks, and recognize how they can improve their responses. For the steps to be used in this way the language will need to be adapted to the class and specific 'answers' will need to be removed.

Teachers have commented that students are more able to be critical of sample responses that are taken from sources outside the classroom, when they cannot be identified. When giving feedback to members of their own class, personal relationships come into play. Students do not feel so able to criticize the work of friends. Classroom cultures may need to be developed where ideas and work may be criticized without individuals feeling threatened and exposed.

Handout 3: Two assessment tasks with assessment frameworks

Golden rectangles

In the 19th century, many adventurers travelled to North America to search for gold. A man named Dan Jackson owned some land where gold had been found. Instead of digging for the gold himself, he rented plots of land to the adventurers.



Dan gave each adventurer four wooden stakes and a rope measuring exactly 100 metres.

Each adventurer had to use the stakes and the rope to mark off a rectangular plot of land.

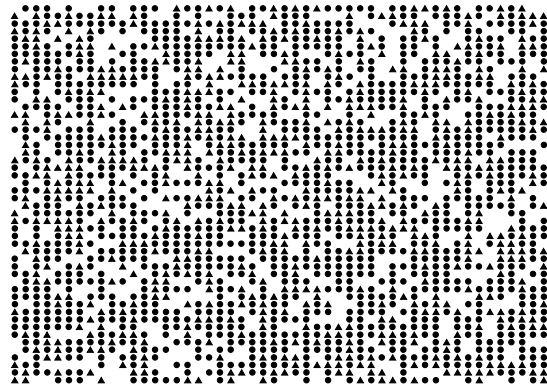
- Assuming each adventurer would like to have the biggest plot, how should he place his stakes? Explain your answer.

Read the following proposition:

“Tie the ropes together! You can get more land if you work together than if you work separately.”

- Investigate whether the proposition is true for two adventurers working together, still using four stakes.
- Is the proposition true for more than two people? Explain your answer.

Counting Trees



This diagram shows some trees in a plantation.

The circles ● show old trees and the triangles ▲ show young trees. Tom wants to know how many trees there are of each type, but says it would take too long counting them all, one-by-one.

- What method could he use to estimate the number of trees of each type? Explain your method fully.
- On your worksheet, use your method to estimate the number of:
 - Old trees
 - Young trees

Assessment framework for Golden rectangles

	Representing	Analysing	Interpreting and evaluating	Communicating
Progress	The student draws one or two rectangles with a perimeter of 100m.	The student works out the areas of their rectangles correctly.	The student draws several rectangles but not a square and the justification is incorrect or omitted.	The work is communicated adequately, but there are gaps and/or omissions.
	Draws several rectangles.	Calculates the areas of their rectangles and attempts to come to some generalisation.	Realises that different shapes have different areas but comes to incorrect or incomplete conclusion.	The work is communicated clearly and the reasoning may be followed.
	Draws several, correct rectangles for an adventurer working alone and for 2 working together. May draw far too many rectangles.	Calculates the areas correctly and finds that a square is best for 1 adventurer and that 2 working together do better than alone.	Attempts to give some explanation for their findings.	The work is communicated clearly and the reasoning may be easily followed.
	Draws an appropriate number of rectangles and collects the data in an organised way.	Calculates the correct areas, finds that a square is best for 1 adventurer and that 2 working together do better than alone. Finds a rule or pattern in their results.	Gives reasoned explanations for their findings.	Explains work clearly and may consider other shapes.

Assessment Framework for Counting Trees

	Representing	Analysing	Interpreting and evaluating	Communicating and reflecting
Progress	Chooses a method, but this may not involve sampling. E.g. Counts all trees or multiplies the number of trees in a row by the number in a column.	Follows chosen method, possibly making errors. E.g. Does not account for different numbers of old and young trees or that there are gaps.	Estimates number of new and old trees, but answer given is unreasonable due to method and errors.	Communicates work adequately but with omissions.
	Chooses a sampling method but this is unrepresentative or too small. E.g. tries to count the trees in first row and multiplies by the number of rows.	Follows chosen method, mostly accurately. E.g. May not account for different numbers of old and young trees or that there are gaps.	Estimates number of new and old trees, but answer given is unreasonable due mainly to the method.	Communicates reasoning and results adequately, but with omissions.
	Chooses a reasonable sampling method.	Follows chosen method, mostly accurately.	Estimates a reasonable number of old and new trees in the plantation. The reasonableness of the estimate is not checked. E.g. by repeating with a different sample.	Explains what they are doing but explanation may lack detail.
	Chooses an appropriate sampling technique.	Follows chosen method accurately. Uses a proportional argument correctly.	Deduces a reasonable number of old and new trees in the plantation. There is some evidence of checking the estimate. E.g. Considers a different sampling method.	Communicates reasoning clearly and fully.

ACTIVITY D: PLAN TO USE PEER AND SELF-ASSESSMENT STRATEGIES

Minimum time needed:	30 minutes before the lesson
	20 minutes for the pre-lesson assessment
	30 minutes to prepare feedback
	60 minutes for the lesson
	15 minutes for reporting back

In this activity, participants plan and carry out a lesson in which students become assessors of their own work (Track A), or assessors of work that we provide for them (Track B). It is helpful if some participants choose to do each track and then they can be compared. A sample lesson plan for each track is provided on **Handout 4**.

- Plan when you will allow students time to tackle an IBL task, individually or in pairs, without your guidance.
- Plan a lesson in which students revisit the task and assess other students' work - either work from their classmates or from some sample responses that you will provide. Make sure students have an opportunity to discuss the importance of the IBL Processes, and sufficient time to revise their own work in the light of the comments.

If you are working on this module with a group, it is helpful if each participant chooses the same assessment task, as this will facilitate the follow-up discussion.

After the lesson meet together to feed back on what happened.

Take it in turns to describe your experiences of using self and peer assessment.

- How did your students perform on the task, unaided?
- How did students assess the provided responses and the work of their peers?
What aspects did they attend to?
- How did students make use of the assessment frameworks?
Did these help students to understand IBL processes?
- How well did students react to and use the evidence to improve their own work?
- What are the implications of this lesson for your future lessons?

Handout 4: A lesson plan in which students are assessors

The following suggestions describe one possible approach to self- and peer-assessment. Students are given a chance to tackle a problem unaided, to begin with. This gives you a chance to assess their thinking and to identify students that need help. This is followed by formative lesson in which they collaborate, reflect on their work and try to improve it.

Before the lesson 20 minutes

Before the lesson, perhaps at the end of a previous lesson, ask students to attempt one of the assessment tasks, *Text messages*, *Golden rectangles* or *Counting Trees*, on their own. Students will need calculators, pencils, rulers, and squared paper.

The aim is to see how able you are to tackle a problem without my help. There are many ways to tackle the problem - you choose. There may be more than one 'right answer'. Don't worry if you cannot understand or do everything because I am planning to teach a lesson on this next in the next few days.

Collect in students' work and review a sample of it. Look carefully at the range of methods students use and the quality of the reasoning. Try to identify particular students who have struggled and who may need support. Also look out for students that have been successful. These may need an extension activity to challenge them further.

Re-introduce the problem to the class 5 minutes

Begin the lesson by briefly reintroducing the problem:

Do you remember the problem I asked you to have a go at last time? Today we are going to work together and try to improve your first attempts. Even if you got most of it right first time, you will learn something because there are different ways to tackle the problem.

At this point, choose between the Track A or Track B. Either decide to let students assess and improve their own work, or offer them the provided samples of work to assess. There won't be time for both!

Track A: Students assess their own work

Track A: Students assess and improve their own work 15 minutes

Ask students to work in pairs or threes and give each group a large sheet of card and a felt-tipped pen. Give each group back their initial attempts at the problem.

I want you to look again at your answers but this time, work as a group. Take it in turns to describe your attempt to the rest of the group. After each suggestion, the others in the group should say what they like about your method and also where they think it can be improved.

After you have all done this, I want you to work together to produce a better answer than you did separately. Make a poster showing your best ideas. It doesn't have to be beautiful, but it should show your thinking.

Go round the room, listening, assessing their thinking and making appropriate interventions. Listen specifically to students that struggled with the task when they worked alone, and offer them support. If students have succeeded and their work is correct, provide one of the planned extensions.

Track A: Students exchange and comment on each others' work 15 minutes

Ask students to exchange their posters with another pair and issue each group with a copy of the "progression steps" framework for the task – one that is written in student-friendly language.

On a separate sheet of paper, write comments on:

- *Representing: Did they choose a good method?*
- *Analysing: Is the reasoning correct – are the calculations accurate?*
- *Interpreting: Are the conclusions sensible?*
- *Communication: Was the reasoning easy to understand and follow?*

As they do this, go round encouraging students to read the work carefully and comment on the points mentioned. You may need to help them understand what the 'progression steps' mean. When students have commented on the work, one person from the group should take the poster to the group that produced it, and explain what needs to be done for the work to be improved.

Track A: Students improve their own work 5 minutes

Give groups a little time to absorb the comments and time to further improve their ideas.

Track A: Plenary discussion on approaches and changes 15 minutes

Towards the end of the lesson hold a discussion on the approaches used and the changes that have been made:

*What changes have you made to your initial work?
Why is it now better than it was before?*

Collect in the work and assess how the thinking has improved.

Track B: Students assess provided sample work

Track B: Students assess provided sample work 15 minutes

Give out the sample student work.

These samples of work were taken from another class. I want you to imagine that you are their teacher. This work may give you ideas you haven't thought of. It is also full of mistakes!

I want you to comment on each of the following themes:

- *Representing: Did they choose a good method?*
- *Analysing: Is the reasoning correct – are the calculations accurate?*
- *Interpreting: Are the conclusions sensible?*
- *Communication: Was the reasoning easy to understand and follow?*

In this way, students will become more aware of what is valued in their work – the Key Processes of representing, analysing, interpreting and communicating.

Listen to their discussions and encourage them to think more deeply. Encourage students to say what they like and dislike about each response and ask them to explain their reasons.

Track B: Students assess sample work using "progression steps" 10 minutes

After students have had time to respond freely, issue each group with a copy of the "progression steps" framework for the task – one that is written in student-friendly language.

*This framework may give you further ideas.
Where would you put the work on the framework?*

Track B: Plenary discussion of the sample work 15 minutes

Project each piece of sample student work on the board and ask students to comment on it:

*What can we say about this piece of work?
Share some of the comments you wrote.*

*What did you think of the methods they chose?
Which method did you like best? Why was this?*

Did you find any mistakes in their work?

Do you agree with their conclusions?

Track B: Working in pairs: Students improve their own work. 10 minutes

Now using what they have learned, ask students to work together to improve their own solutions. As they do this, as students to explain their thinking.

Max, tell me what you have done to improve your own solution.

ACTIVITY E: DISCUSS STRATEGIES FOR DIFFERENTIATION

Time needed: 20 minutes

Reflect on your normal teaching practices. When you assess classes, you begin to realize the considerable individual differences in students and they have very different learning needs. Some students need more support, while others need a greater challenge.

- How do you normally deal with range of different learning needs of your students?
- Discuss the advantages and disadvantages of the four strategies shown on **Handout 5**.
- Compare your views with the comments given on **Handout 6**.

Handouts 5 and 6: Meeting the needs of all students

<p>Assessment reveals that all students have different learning needs. How do you respond to this in your normal lessons?</p> <p>Discuss and note down the advantages and disadvantages of each approach. Add your own ideas underneath.</p> <div style="border: 1px solid black; padding: 5px;"> <p>Differentiate by quantity? When students appear successful, you provide them with a new problem to do.</p> <p>.....</p> <p>.....</p> <p>.....</p> </div> <div style="border: 1px solid black; padding: 5px;"> <p>Differentiate by task? You try to give each student a problem that is matched to their capability.</p> <p>.....</p> <p>.....</p> <p>.....</p> </div> <div style="border: 1px solid black; padding: 5px;"> <p>Differentiate by outcome? You use open problems that encourage a variety of possible outcomes.</p> <p>.....</p> <p>.....</p> <p>.....</p> </div> <div style="border: 1px solid black; padding: 5px;"> <p>Differentiate by level of support? You give all students the same problem, but then offer different levels of support, depending on the needs that become apparent.</p> <p>.....</p> <p>.....</p> <p>.....</p> </div>	<p>Differentiate by quantity? <i>When students appear successful, you provide them with a new problem to do.</i></p> <p>This approach is common, but it leads to students viewing the curriculum as a list of problems to do, rather than processes to acquire. This approach will not promote reflection on alternative methods for doing a problem - different ways of representing, analysing, interpreting and communicating.</p> <p>Differentiate by task? <i>You try to give each student a problem that is matched to their capabilities.</i></p> <p>But how does one know if a problem is suitable? We can only match a problem to a student if we have a profound understanding of both. Our view of the problem is usually based on our own way of doing it – and there may be many other approaches. We also have an imperfect and often prejudiced view of students' capabilities. We so easily judge students' 'mathematical ability' by their ability to carry out routine procedures they have recently been taught. Problem solving requires a different set of skills and may result in different students performing well. This approach also creates management difficulties as different problems are used with different students. This reduces possibilities for whole class discussions and sharing knowledge.</p> <p>Differentiate by outcome? <i>You use more open problems that encourage a variety of possible approaches and outcomes.</i></p> <p>This approach requires problems and situations that allow for such a variety to emerge. The Bowland problems are like this, but they do make considerable demands on students who are unfamiliar to problem solving. Many teachers comment that as soon as students begin to struggle, they want to 'leap in', 'take over' and structure the problem, so that students have clear steps to follow. This tendency undermines the very purpose of the lesson – to develop students' ability to use Key Processes in an autonomous way. On the other hand, too little guidance may result in prolonged failure and frustration. Some teachers therefore make it a rule that students should always help and share ideas with each other, before asking for help from the teacher.</p> <p>Differentiate by level of support? <i>You give all students the same problem, but then offer different levels of support, depending on the needs that become apparent.</i></p> <p>This approach avoids many of the difficulties described above. The support may be by other students, or by the teacher - orally, or in written form. In the lessons we have suggested, the teacher asks the students to attempt what they can unaided, then they are offered the support of their peers as ideas and approaches are shared and discussed. If further support is needed, then the teacher may supply this through questions that cause students to attend to particular features of the problem, or through more specific hints. Timing such help is critical. One of the important goals of problem solving is to allow students the experience of <i>struggling</i> with a problem for some time and experiencing the sense of achievement that arrives when the problem has been overcome. If we help students too quickly, we rob them of this experience.</p>
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The strategies suggested on **Handout 5** are:

- *Differentiate by quantity?* When students appear successful, you provide them with a new problem to do.
- *Differentiate by task?* You try to give each student a problem matched to her capability.
- *Differentiate by outcome?* You use open problems that have a variety of possible outcomes.
- *Differentiate by level of support?* You give all students the same problem, but offer different levels of support, depending on the needs that become apparent.

The first two of these approaches are unhelpful, particularly when developing IBL processes, for the reasons identified in Handout 6. IBL tasks are 'open' in the sense that they encourage a variety of approaches. Their difficulty is not merely related to their apparent 'content', but is also related to the familiarity of the context, the complexity of information within the problem, the connections that need to be made, the length of the chains of reasoning required, and so on.

Helping students that struggle

As well as finding the tasks challenging, students may find the whole idea of self and peer assessment difficult. They are being asked to reflect on the methods and processes that they and others have used. Think again about your lessons using the IBL tasks.

- How might you help those who struggle with the task?
- How can you help those who struggle with the whole idea of peer assessment?

Teachers have found that when students get stuck with a task, then they may be considerably helped by:

- discussing their difficulty with a partner (not necessarily their neighbour);
- looking at examples of other students' work (however rough) - these will suggest new ways to access and approach the task.

As soon as the teacher gives detailed guidance on what to do, the students are unable to make strategic decisions for themselves. Such guidance should therefore only be given as a last resort, after students have been allowed to struggle and help each other.

We have found that most students enjoy and value self and peer assessment. Some however, may be unused to revisiting tasks and reflecting on earlier work and may not therefore appreciate the value of discussing different solution methods in depth. "When I know the answer, what point is there in discussing the problem further and looking at other people's work?" Such students prefer to 'get on' and tackle new tasks. We have found that it is important to carefully explain the purpose of peer assessment to students meeting it for the first time.

Stretching students that succeed

Some students may have done very well at the problems, even at the very beginning. Others may have worked well and finished quickly. It is a good idea to plan for such eventualities.

Think back to your own lesson.

- When students succeeded, how did you extend their thinking?
- What alternative approaches to the task did you, or could you suggest?
- What extensions to the task did you, or can you suggest?

Even if students succeed in the problems, they can still learn a great deal by revisiting them.

Students may be encouraged to:

- find alternative or more elegant ways of representing and tackling the task;
- make up their own variants or extensions to tasks
- devise their own "progression steps", to develop their understanding of Key Processes.

You may be like to suggest your own possible extensions to the tasks. For example:

- *Text Messaging*: How long would it take to spread a piece of news around the school if each person sends a text message to four other people?
- *Counting Trees*: What method would you use if you were asked to estimate the number of beans in a jar?
- *Golden rectangles*: Suppose the adventurers were only given three stakes each? (The task would need to be renamed: *Golden triangles*).

SUGGESTED FURTHER READING

Black, P., & Wiliam, D. (1998). *Inside the black box: raising standards through classroom assessment*. King's College London School of Education.
Now published by GL Assessment: <http://shop.gl-assessment.co.uk>

This short booklet offers a summary of the extensive research literature into formative assessment. It shows that there is clear evidence that improving formative assessment raises standards, and offers evidence showing how formative assessment may be improved. This booklet is essential reading for all teachers.

Black, P., & Harrison, C. (2002). *Working inside the black box: Assessment for learning in the classroom*. King's College London School of Education.
Now published by GL Assessment: <http://shop.gl-assessment.co.uk>

In this booklet, the authors describe a project with teachers in which they studied practical ways of implementing formative assessment strategies and the effect this had on learning. The section on peer-assessment and self-assessment (pages 10-12) are particularly relevant to this module.

Black, P., Harrison, C., Lee, C., Marshall, B., & Wiliam, D. (2003). *Assessment for learning: Putting it into practice*. Buckingham: Open University Press.

This book gives a fuller account of the earlier booklets *Inside the black box* and *Working inside the black box*. It discusses four types of action: questioning, feedback by marking, peer- and self-assessment and the formative use of summative tests. The section on peer and self-assessment (pp 49-53) is particularly relevant to this module.

Hodgen, J., & Wiliam, D. (2006). *Mathematics inside the black box*. King's College London School of Education. Now published by GL Assessment: <http://shop.gl-assessment.co.uk>

This booklet applies the above findings specifically to Mathematics. It considers some principles for Mathematics learning, choice of activities that promote challenge and dialogue, questioning and listening, peer discussion, feedback and marking, and self and peer assessment. This booklet is essential reading for all mathematics teachers. Pages 9-10 are particularly relevant to this module.